1. Define the term “conjugate action.”
its significance for design of power transmission systems.

“Conjugate action” is the property of a transmission that delivers constant rate of rotation of the output shaft if rate of rotation of the input shaft is also constant. It is important to note that this not not simply valuable in and of itself, but is also a requirement for smooth transmission of power. It reduces vibration, noise, and premature failure due to fatigue of the machine elements.

2. You fill a one liter container with air at 60 psi gauge pressure and plan to use it as a source of power for a machine. The air in the bottle is at thermal equilibrium with the air in the room at 20 degrees Centigrade. Estimate (within ±10% is fine) the force applied if a valve is opened connecting the reservoir of air to a piston with a one inch internal diameter and a two inch stroke assuming the piston extends its full stroke in about 2 seconds.

Dislacement of the piston

Since the piston is only 2% of the volume of the reservoir and we only need an estimate with 10%, it’s good enough to just multiply the original gauge pressure times the area of the face.

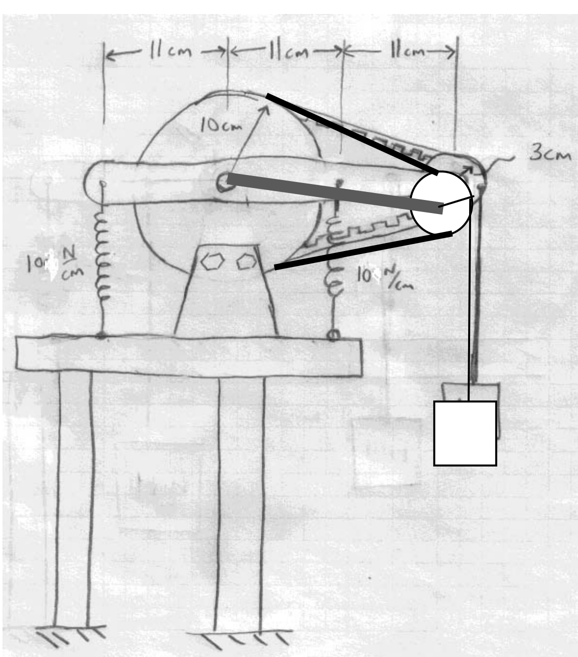
$$\frac{\pi}{4}\cdot(1\cdot in)^2\cdot 2\cdot in = 0.026L$$

$$\frac{\pi}{4}\cdot(1\cdot in)^2\cdot 60\, psi = 47.124 lbf \qquad \frac{\pi}{4}\cdot(1\cdot in)^2\cdot 60\, psi = 209.618N$$

3. Sketch the mechanism in a position that places it in static equilibrium. Base your drawing on an estimate of the displacements to within ± 20%. Assume the joints have negligable friction and that the pulleys and links have negiligable weight. The 10 cm radius pulley is fixed with respect to the table and cannot rotate. You can assume the toothed belt will not slip. The extension springs are at their natural length. You may assume that the extension springs apply tension with the spring constant indicated but cannot apply any appreciable force in compression (they buckle). Briefly justify your solution with a couple equations, schematic diagrams, and/or a few sentences of explanation. Be sure to indicate clearly:
   - Whether you think the 3cm pulley rotates clockwise or counterclockwise
   - Whether you think the arm connecting the pulleys rotates clockwise or counterclockwise
   - Whether you think the arm 1 kg mass is higher or lower at equilibrium than at the starting position

Consider a modest clockwise rotation of the arm, say 0.1 radian (6 deg). To maintain the proper position of the belt, tangent to both pullleys, the belt will have to wrap arong the top of the 10 cm rad pulley by 10cm*0.1 rad or 1cm. The kinematics of a belt drive demand that the same 1cm of belt feeds off of the 3cm pulley which requires a 1cm/3cm=0.33 rad (18 deg) rotation of the 3cm dia pulley relative to the arm or 0.23 with respect to the fixed frame of reference.

This 0.1 deg rotation of the arm would also extend the left spring by 1.1cm leading to a 11N downward foce. The extension spring on the right side is placed in compression and we assume it buckles out of the way or othjerwise goes slack and applies negligable force.

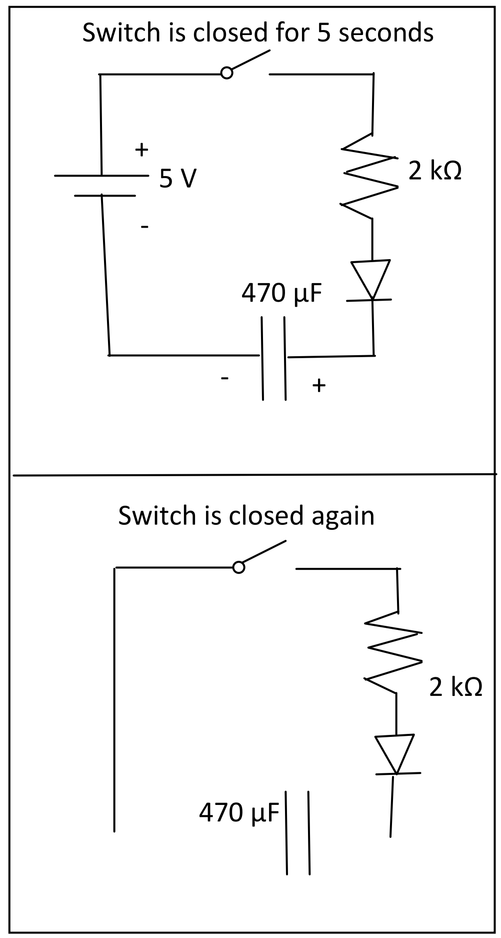


Due to the small angles and generous ± 20% allowance for our estimate, we can linearize. We have a motion of the weight due to two factors:
Rotation of the arm => 0.1 rad*24*cm=2.4 cm downward
Rotation of the 3cm pulley => 0.33 rad*3cm=1cm upward
So a net motion of 1.4 cm downward.

Kinematically, the pulley arrangement is similar to attaching the weight directly to the arm at 14 cm. I infer the guess of 0.1 rad of rotation was a bit low. I update my guess by 30% throughout to:

0.13 rad (7.5deg) <u>CW rotation of the arm</u>
0.23 rad (17deg) <u>CCW rotation of the 3cm pulley</u>
net motion of <u>1.8 cm downward of the 1 kg mass</u>
as a check I see if the energy stored in the spring equals the energy lost by the mass mgh=0.18J
0.5*K*x^2=0.5*10*(N/cm)*(0.13*11cm)^2=0.19J close enough.

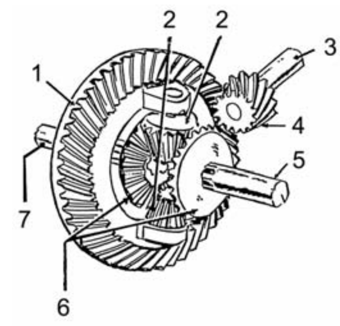
4. The components shown here (resistor, LED, capacitor, battery, and switch) are connected in series. The switch is closed for 5 seconds. During that time, the LED lights and then gradually dims. The circuit composed of the very same components is then reconfigured and reconnected as shown. The switch is then closed. Which statement best describes what happens after the switch is closed again:



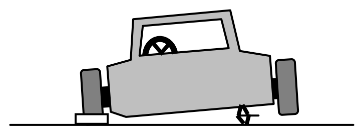
a) The LED lights up and then slowly dims over the course of 5 seconds
b) The LED starts dim then slowly brightens over the course of 5 seconds
c) The LED lights up steadily
d) <u>LED does not light</u>

The capacitor was left in the same orientation this time whereas it was reversed previously between charging and discharging. In this case, in the new problem, the capactor cannot dischage at all due to the orientation of the diode.

5. Consider a rear wheel drive vehicle with a four speed manual transmission connected to a conventional differential (such as the one depicted to the right). The vehicle is placed in first gear, the engine is turned off.

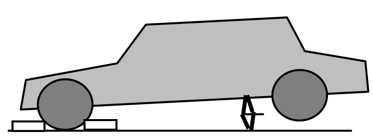


A) The front and rear driver's side rear tires are "chocked" by placing wedges in front and behind them. A jack is used to raise the passenger's side tires slightly off the ground. Using your hands, you apply a clock-wise torque to the passenger's side rear tire. Briefly describe what you think will happen.



With the engine off and the manual transmission in first gear, the drive shaft into the differential will be fixed. With the driver's side wheel chocked, it is also fixed. The differential has 2 kinematic DOF so it has been frozen and the passenger's side wheel cannot be turned by hand.

B) Again, the engine is off and the manual transmission is in first gear. The front tires are chocked and a jack is used to raise BOTH the rear tires slightly off the ground. Using your hands, you apply a clock-wise torque to the driver's side rear tire. Briefly describe what you think will happen.



Again, with the engine off and the manual transmission in first gear, the drive shaft into the differential will be fixed. With the driver's side wheel up in the air now, it is free to turn. If you apply a torque and turn by hand either rear wheel, the opposite side will also turn BUT IN THE OPPOSITE DIRECTION. So you'll observe CCW rotation of the passenger's side wheel.

6. The subproblems below refer to the page from a bearing catalog provided here.

A) iIf gear PX24B-8 and PX24B 22 are mated together in a gear train, how far apart should the centers of their shafts be placed?

(0.333+0.916)/2=

0.625 inches apart

B- 22 are mated together in a gear train and a torque of 2 ft lbs is applied to PX24B-8, what is the separation force?

24 inch lbs / radius of 0.333/2 leads to a <u>tangential</u> force of

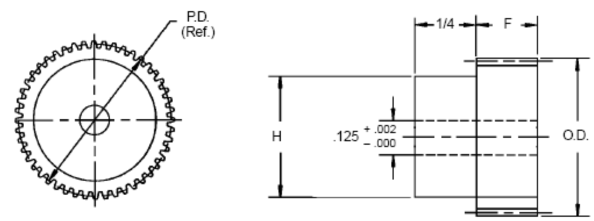
144 lbs.

To get separation force, multiply by tan(20deg)

= 52.5lbs

Spur Gears

24, 32, 48, and 64 Pitch 1/8" Bore AGMA Quality 4
Cold Rolled Steel and Brass 20° Pressure Angle



B 9

COLD ROLLED STEEL C12L14 OR C12L15 WITH SELENIUM	BRASS ALLOY 360					
STOCK NUMBER	STOCK NUMBER	NO OF. TEETH	PITCH DIA.	OUTSIDE DIA.	H	F
24 PITCH (.1309)						
PX24S-8	PX24B-8	8	.333	.416	.208	1/4
PX24S-9	PX24B-9	9	.375	.458	.250	
PX24S-10	PX24B-10	10	.417	.500	.291	
PX24S-12	PX24B-12	12	.500	.583	.375	
PX24S-16	PX24B-16	16	.666	.750	.542	
PX24S-18	PX24B-18	18	.750	.833	.625	
—	PX24B-22	22	.916	1.000	.792	
32 PITCH (.0981)						
PX32S-10	PX32B-10	10	.312	.375	.218	1/4
PX32S-11	PX32B-11	11	.344	.406	.250	
PX32S-12	PX32B-12	12	.375	.437	.281	
PX32S-14	PX32B-14	14	.438	.500	.343	
PX32S-15	PX32B-15	15	.469	.531	.375	
PX32S-16	PX32B-16	16	.500	.562	.406	
PX32S-18	PX32B-18	18	.563	.625	.468	
PX32S-20	PX32B-20	20	.625	.688	.532	
	PX32B-24	24	.750	.813	.656	
48 PITCH (.0654)						
PX48S-14	PX48B-14	14	.292	.333	.229	1/8
PX48S-15	PX48B-15	15	.312	.353	.250	
PX48S-16	PX48B-16	16	.333	.375	.271	
PX48S-18	PX48B-18	18	.375	.417	.312	
PX48S-24	PX48B-24	24	.500	.542	.437	
PX48S-32	PX48B-32	32	.666	.708	.604	
	PX48B-36	36	.750	.792	.687	
	PX48B-40	40	.833	.875	.770	
64 PITCH (.0490)						
PX64S-15	PX64B-15	15	.234	.265	.187	1/8
PX64S-16	PX64B-16	16	.250	.281	.203	
PX64S-18	PX64B-18	18	.281	.312	.234	
—	PX64B-24	24	.375	.406	.328	
—	PX64B-40	40	.625	.656	.578	
—	PX64B-48	48	.750	.781	.703	

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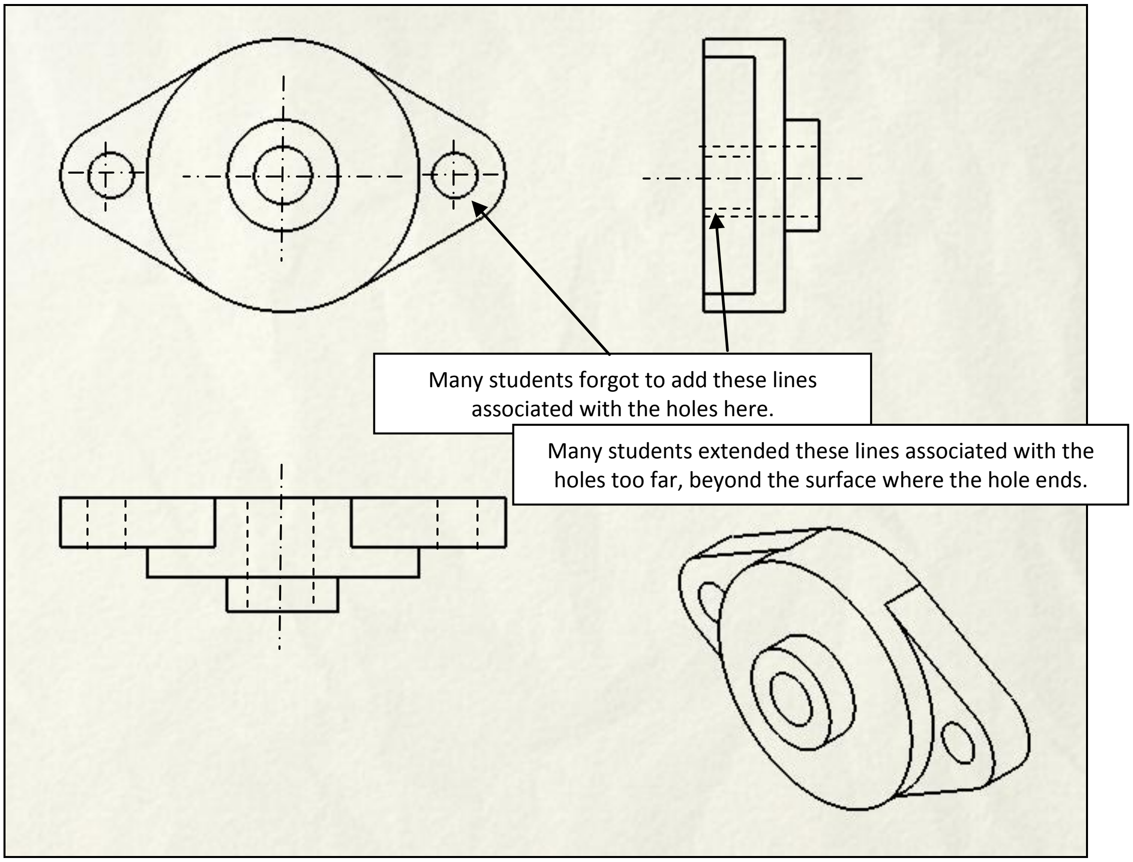
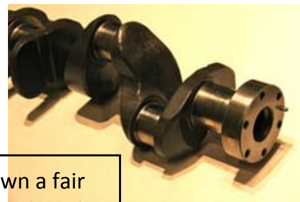
C) If gear PX 24B-8 and PX24B-22 are mated together 0.02 inches farther apart than you determined in part A, what are the primary consequences? Would your answer to part B change and if so would it rise or fall?

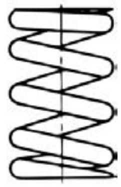
Such as mall displacement with leave the gears in mesh still. Not much of a problem. Mainly the backlash would increase. Conjugate action would be preserved. The separation force would rise a small amount due to the larger pressure angle as the gears mesh at point farther from the gear's centers.

7. Add hidden lines and center lines to the views below.

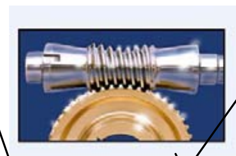


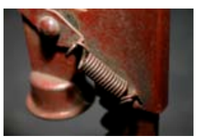
8. Match the items below to the terms that describe them.

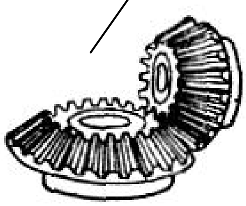


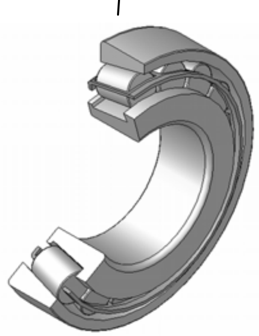


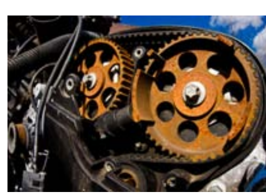
The crank shaft seems to have thrown a fair number of people off. Many students thought it might be a cam shaft. The lobes on this item aren't cams, but rather counterweights.

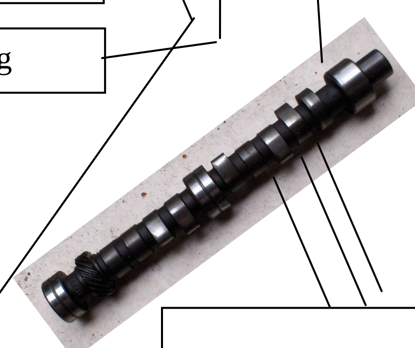












- Torsion spring
- Extension spring
- Tapered roller bearing
- Bevel gear
- Cam shaft
- Worm gear
- V belt pulley
- Constant force spring
- Crank shaft
- Compression spring
- Timing belt pulley
- Rack
- Ball bearing

here are cams.

These features on a timing belt pulley engage with the teeth on a toothed belt.

9. vehicle is composed of a box shaped structure with permanent magnet DC motors placed at all four corners and driving all four wheels (through a gear train). All these motors are attached to a 5V NiCad battery pack. The vehicle is climbing a 20 degree incline. The vehicle is proceeding very slowly since the motors are nearly stalled. The coefficient of static friction between the wheels and the inclined surface is 50% greater than that needed to maintain a steady climb up that grade. At a particular moment, the mass of the vehicle is reduced by 25% because a robot arm on the vehicle takes an object off the vehicle and lays it to the side. Circle the item below that best describes the events that would likely transpire.

a) The vehicle will continue up the ramp at the same speed as before.
b) The normal force of the wheels on the surface will decrease causing the wheels will to begin to slip with respect to the surface of the incline reducing the vehicle's speed.
c) The vehicle's velocity will increase instantaneously when the block is released so that the vehicle's momentum will remain constant even as the mass is reduced.
d) <u>The vehicle will accelerate smoothly up the ramp until it reaches a higher steady-state velocity.</u>
e) The wheels will not slip but will turn backwards causing the vehicle to go back down the ramp.

e. The phrase "velocity will increase instantaneously" should be a cue that something is wrong. A body cannot increase in speed "instantaneously" unless a huge force is applied for a very short period, such as a bullet in the chamber of a pistol. The phrase "the vehicle's momentus remains constant even as the mass is reduced" also must have sounded attractive. Indeed, a system of bodies will have a constant total momentum when there is no net external force applied. In this case, the block that is dropped would have its share of the system's momentum and would initially keep moving at the same velocity as the robot. Subsequently, it could have significant forces aplied to it by the ramp to stop it, but this would not cause the robot to accelerate to make up for its lost momentum since there are no forces between the two bodies once released.

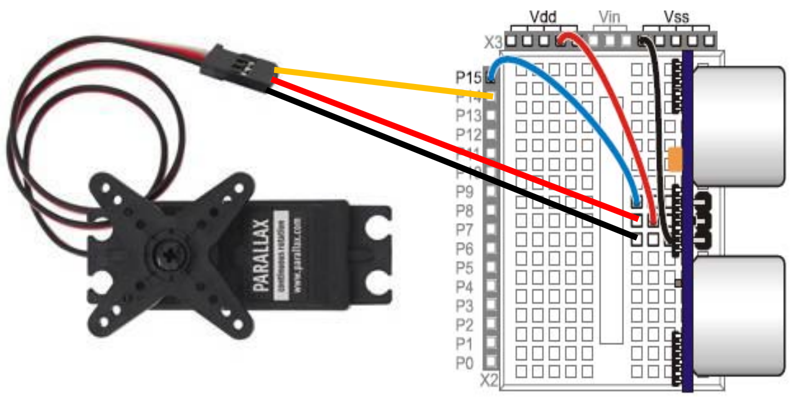
10. Explain why a lead acid battery is a reasonable choice for use in typical commercially available automobiles today, but may not be a reasonable choice for a plug-in electric vehicle.

The high power density of lead acid batteries is useful for starting a car since it takes a lot of power to turn over a cold engine. The low energy density is not a big deal for most cars today because you don't take much time to start the car (1 sec of cranking?), so the battery doesn't have to be so large and is a small fraction of the weight of the car anyway. It helps too that lead acid batteries perform well at cold temperatures. The low number of cycles to failure is not usually a problem because starting is really not a cycle. Letting the battery go fully dead is bad practice. –

For a plug-in electric car, the demands on the battery are very different. You need much greater energy density and far more cycles of charging and re-charging. The speed of charging might be an issue also, although some people propose that plug-in vehicles should have batteries swapped in and out rather than charging on the car and tying up that valuable asset waiting for the charge to complete.

11. A Homework board is wired with an ultrasonic sensor and a continuous rotation servo as shown below and the code below has been uploaded onto the EEPROM. The sensor points forward on the vehicle and the servo is configured to drive the wheels.

```
time VAR Word
speed VAR Word
LABEL1:
PAUSE 14
PULSOUT 15, 5
PULSIN 15, 1, time
IF (time<150) THEN
' time of 150 is about two inches
  PULSOUT 14, 750
' this sends a 1.5 millisec pulse which will
command the servo to remain still
  GOTO LABEL1
ELSE
  GOTO LABEL2
ENDIF
LABEL2:
PULSOUT 15, 5
PULSIN 15, 1, time
IF (time>450) THEN
 PULSOUT 14, 1000
' command the servo to go forward
ELSEIF (time<300) THEN
  PULSOUT 14, 500
 ' command the servo to go backward
ELSE
 PULSOUT 14, 750
 ' command the servo to remain still
ENDIF
PAUSE 14
GOTO LABEL2
```



This code would have the vehicle wait and idle as long as a barrier (the door of the robot's house?) is no more than 2 inches from the front of the vehicle. Once that barrier is removed, the vehicle would drive forward until it meets an object. It should stop when the object (the rail of the contest field?) is 6 inches from the nose and wait. If subsequently, something new (a botherbot?) is placed between the vehicle and the object, the vehicle backs up to seek a 4 inch spacing. So the polite little bot will step aside for the bother bot. Then it wil close up the gap again to place the rail 6 inches away again.